

Wave Oscillations

SHM $\ddot{x} + \omega_0^2 x = 0, \omega_0 = 2\pi f_0 = \sqrt{\frac{k}{m}}$
 $E = E_P + E_K, \frac{dE}{dt} = 0$

Damped $\ddot{x} + 2\gamma\dot{x} + \omega_0^2 x = 0, \gamma = \frac{b}{2m}, \omega^2 = \omega_0^2 - \gamma^2$
 $\Rightarrow x = Ae^{(-\gamma \pm i\omega)t}$ (b is damping constant)
Light $\omega_0^2 > \gamma^2$, Heavy $\omega_0^2 < \gamma^2$, Crit $\omega_0^2 = \gamma^2$
 $E = E_0 e^{-2\gamma t}, \tau = \frac{1}{2\gamma}, Q = \frac{\omega_0}{2\gamma} = \frac{\omega_0}{\Delta\omega}$

Super-position $A(t) = \cos(\omega_1 t) + \cos(\omega_2 t)$
 $= 2(\cos(t \frac{\omega_1 + \omega_2}{2}) \cos(t \frac{\omega_2 - \omega_1}{2}))$

Electrostatics

Force / Field $\underline{F} = \frac{Qq}{4\pi\epsilon_0 r^2}, \underline{E} = \frac{F}{q} = \frac{Q}{4\pi\epsilon_0 r^2}$

Potential Δ $dV = \frac{dU}{q} = -\underline{E} \cdot d\underline{l}, V = -\int_{\infty}^r \underline{E} \cdot d\underline{l}$

Gauss $\phi_E = \int_S \underline{E} \cdot d\underline{A} = \frac{Q}{\epsilon_0}$

Conductors $\underline{E} = \underline{0}$ everywhere
All charge on outer surface
No net charge in inner surface

Capacitance $C = \frac{Q}{V} = 4\pi\epsilon_0 R = \frac{\epsilon_0 A}{d}$
 $U_E = \frac{1}{2} CV^2 = \frac{1}{2} \epsilon_0 E^2 V$

Magnetostatics

Force $\underline{F} = q(\underline{E} + \underline{v} \wedge \underline{B}),$ motor effect = RH

Ampere's $\int_C \underline{B} \cdot d\underline{l} = \mu_0 I \Rightarrow B = \frac{\mu_0 I}{2\pi r}$ (infinite wire)

Flux $\phi_m = \int_S \underline{B} \cdot d\underline{A}$ (closed surface = 0)

Inductor $V_E = \int_C \underline{E} \cdot d\underline{l} = -\frac{d\phi_m}{dt}, L = \frac{\phi_{threading}}{I}$
 $U_B = \frac{1}{2} LI^2 = \frac{1}{2} \frac{B^2}{\mu_0} V$

Electrical Circuits

Complex $Z_C = \frac{1}{i\omega C}, Z_L = i\omega L$

Oddments $V_{RMS} = \frac{V_0}{\sqrt{2}}, \omega_0 = \frac{1}{\sqrt{LC}}$

Waves

Basics $k = \frac{2\pi}{\lambda}, c = \lambda v, \psi = A \cos(\omega t + kx)$
 $\psi = A \cos(\omega t + kx), \frac{\partial^2 \psi}{\partial x^2} = \frac{1}{c^2} \left(\frac{\partial^2 \psi}{\partial t^2} \right)$

String $C = \sqrt{\frac{T}{\rho}}, E_{density} = \frac{1}{2} \rho \left(\frac{\partial \psi}{\partial t} \right)^2 + \frac{1}{2} T \left(\frac{\partial \psi}{\partial x} \right)^2$

Standing $\psi = A \cos(k_x x) \cos(\omega t)$

EM Waves $\int_C \underline{B} \cdot d\underline{l} = \mu_0 \epsilon_0 \frac{d\phi_E}{dt}, c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$

Optics

Tiny Slit $A = 2A_0 \cos^2(k \frac{d}{2}) \sin \theta \cos(\omega t - kr)$

Finite Slit $A = A_{max} \sin c \left(\frac{\phi}{2} \right)$

Two Slits $A = A_{max} \sin c \left(k a \sin \left(\frac{\phi}{2} \right) \right) \cos \left(k \frac{d}{2} \right) \sin \phi$

Refraction $\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1},$ TIR for $\sin > 1$

Lenses $\frac{1}{u} + \frac{1}{v} = \frac{1}{f} = \left(\frac{n_2}{n_1} - 1 \right) \left(\frac{1}{R_1} + \frac{1}{R_2} \right), P = \frac{1}{f}$

Wave-Particle Duality

Basics $\lambda = \frac{h}{p}, E = h\nu$

Photoelectric $K_{MAX} = h\nu - W = h(\nu - \nu_0)$

Compton $\lambda' - \lambda = \frac{h}{m_e c} (1 - \cos \theta)$

Evidence Davidson-Germer (electron scattering from crystallised surface showed diffraction)
G.P. Thompson (electrons on metal foil shows diffraction rings)